

A power plant to be built on a river having rate of flow of 67 m<sup>3</sup>/s and utilizing 12.8 m of head. The speed fixed by the electrical company is 180 rpm. The efficiency of the turbine is 90%. It is further seen that the specific speed of 342 rpm would be best for the hydro plant. Selection of water turbine is to be made from the following data meant for the required specific speed and calculated for the unit speed.

Diameter of the runner (cm)	137.5	145	152.5	160	167.5
Unit Speed in rpm	49.5	47	44.6	42.5	40.6
Unit Power in kW	35.4	39.5	43.6	48.1	53.7

Find out (i) the type of the turbine (ii) number of the turbine required (iii) diameter of the runner based upon unit power.

H = 12.8 m  
 Q<sub>total</sub> = 67 m<sup>3</sup>/s  
 N = 180 rpm  
 N<sub>s</sub> = 342  
 η<sub>t</sub> = 90 %

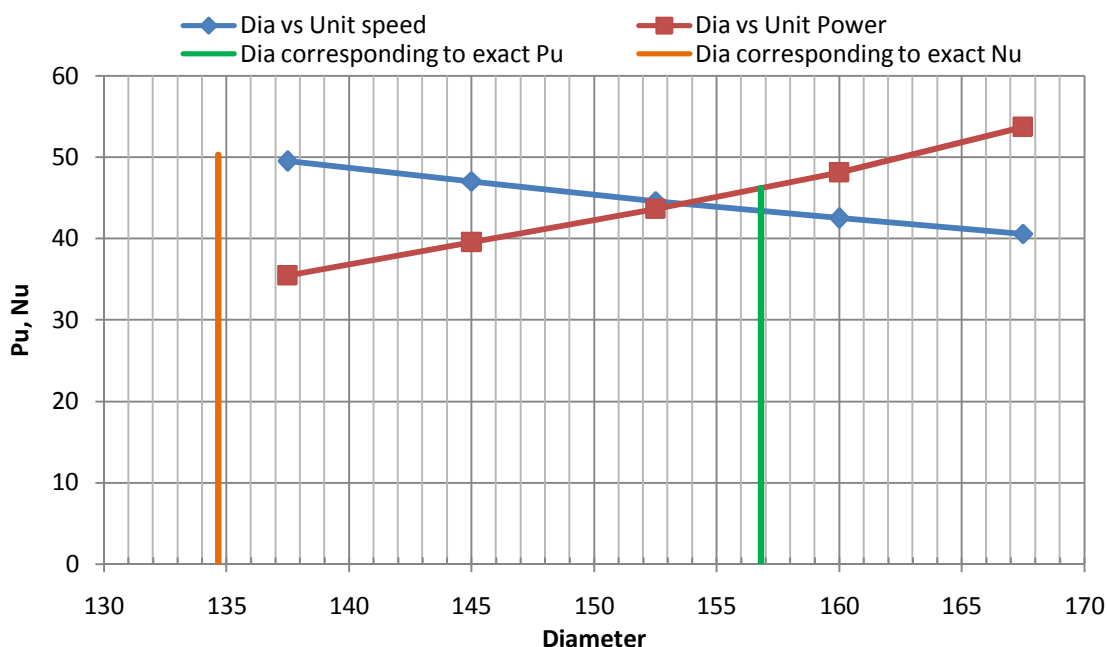
from specific speed  $N_s = NP^{0.5}/H^{5/4}$

Pt per turbine = 2116.1 kW  
 Unit power P<sub>u</sub> = 46.21 kW/m<sup>1.5</sup>  
 unit speed N<sub>u</sub> = 50.3 rpm/m<sup>0.5</sup>

Type of the runner is Kaplan  
 Per Turbine discharge Q = 18.725 m<sup>3</sup>/s (Pt = η<sub>t</sub>γQH)  
 Number of Unit = (Q<sub>total</sub>/Q) 3.5782 approx 4

pp-89, Jagdish Lal

IF(N<sub>s</sub> ≥ 225, "Kaplan", IF(N<sub>s</sub> ≥ 51, "Francis", "Pelton"))



for the above unit power (Pu) **156.8** cm  
diameter of the runner can be  
calculated from the above table

	before	after
dia(cm)	152.5	160.0
Pt(kW)	43.6	48.12

graph (Pu)

156.80	0
156.80	46.21

for the above unit speed (Nu) **134.65** cm  
diameter of the runner can be  
calculated from the above table

	before	after
dia(cm)	145	152.5
Ns	47.0	44.60

graph (Nu)

134.65	0
134.65	50.31

2. The result of a test on water turbines operating at full gate opening under a head of 5.28 m are given as follows:

Unit Speed	65.4	72.6	76.3	79.9	83.5	87.2	90.75	94.4
Q (m <sup>3</sup> /sec)	3.74	3.66	3.6	3.56	3.51	3.45	3.39	3.32
Unit power in kW	12.53	12.87	13.00	13.02	12.92	12.73	12.38	11.94

Plot graphs of unit power (kW) and efficiency against unit speed. If the turbine runs at a speed of 200 rpm, find the power and efficiency. If the head is increased to 5.8 m, the speed remains the same, find the corresponding power and efficiency.

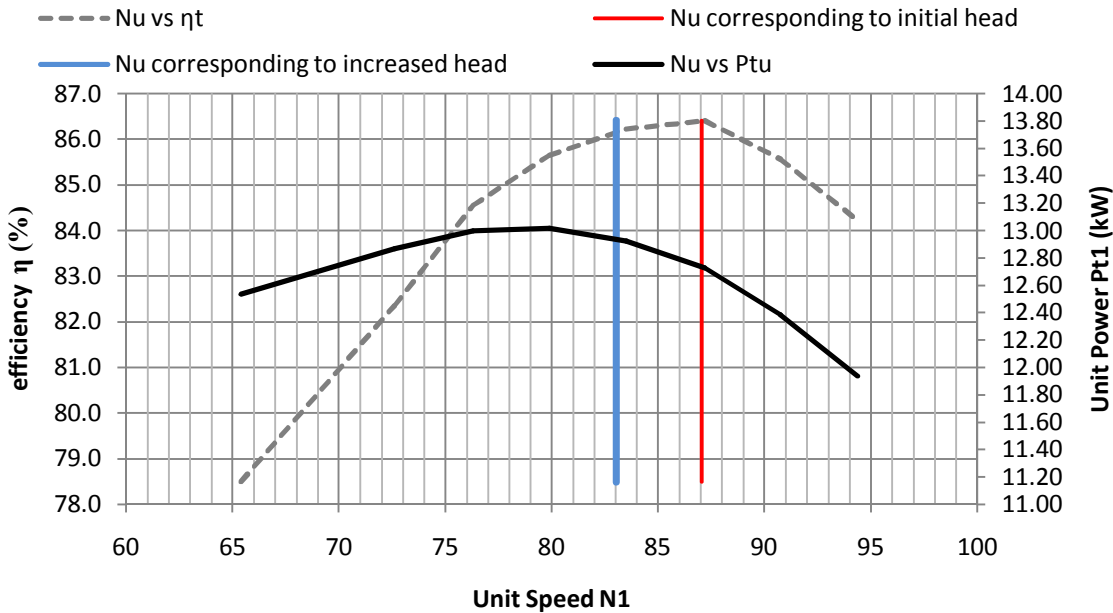
1 hp = 0.746 kW

Given:

H= 5.28 m  
N= 200 rpm  
new H= 5.8 m

$\gamma$ = 9810 N/m<sup>3</sup> or 1000 when in HP  
turbine output  $P_t = P_u \cdot H^{3/2}$   
turbine available power  $P_a = \gamma QH$  (W) or  $P_a$  (HP) =  $\gamma QH/75$   
Turbine efficiency  $\eta_t = (P_t/P_a)$  (=1000\*( $P_u \cdot H^{0.5}$ )/ $\gamma Q$ ) (=75\*( $P_u \cdot H^{0.5}$ )/ $\gamma Q$ )

$\eta_t$	78.5	82.4	84.6	85.7	86.2	86.4	85.6	84.2
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When N= 200 rpm  
unit speed  $N_u$ = 87.0 rpm  
find values of unit power  $P_{t1}$  and efficiency  $\eta_t$  from figure

graph (initial head)	
87.0	78.5
87.0	86.4

unit power  $P_{tu}$  = 12.5 kW/m<sup>1.5</sup>  
Turbine output  $P_t$  = 151.7 kW or 203.3 HP  
efficiency  $\eta_t$  = 83.5 %

if head is increased

H = 5.8 m  
When N = 200 rpm  
unit speed  $N_u$  = 83.0 rpm

find values of unit power  $P_{t1}$  and efficiency  $\eta_t$  from figure

unit power  $P_{tu}$  = 12.9 kW/m<sup>1.5</sup>  
Turbine output  $P_t$  = 180.2 kW or 241.5 HP  
efficiency  $\eta_t$  = 86.2 %

graph (increased head)

83.0	78.5
83.0	86.4



The head water surface and tail water surface levels in a water turbine installation are 51 m and 45 m above sea level respectively. The turbine is designed to run at a uniform speed of 75 rpm under all conditions. The manufacturer's test under a head of 7.5 m shows that the turbine develops 1500 kW at its maximum efficiency of 87%. The computed values of unit speed and unit power in percentage of normal values and the efficiency  $\eta$  in percentage of the maximum efficiency are tabulated below:

Unit Speed in % of normal value	65.4	70	80	90	100	110	120	130
Unit power in % of normal value	73.5	82.2	90	96.5	100	99.5	99	90
efficiency $\eta$ in % of normal value	85	88	94	98	100	99	94	85

Calculate the power and discharge of the turbine under normal working conditions.

Given:

$$1 \text{ hp} = 0.746 \text{ kW}$$

$H_{\text{test}}$	7.5	m
$P_{\text{t test}}$	1500	kW
$\eta_{\text{testmax}}$	87	%
head water surface	51	m
tail water surface	45	m
design $N_{\text{Normal}}$	75	rpm

$$\gamma = 9810 \text{ N/m}^3 \quad \text{or } 1000 \text{ when in HP}$$

$$\text{turbine output } P_t = P_u \cdot H^{3/2}$$

$$\text{turbine available power } P_a = \gamma Q H \text{ (W)} \quad \text{or} \quad P_a \text{ (HP)} = \gamma Q H / 75$$

$$\text{Turbine efficiency } \eta_t = (P_t / P_a) \quad (= 1000 \cdot (P_u \cdot H^{0.5}) / \gamma Q) \quad (= 75 \cdot (P_u \cdot H^{0.5}) / \gamma Q)$$

$$\text{tested unit power } P_{\text{utest}} = 73.0 \text{ kW/m}^{1.5}$$

$$\text{tested unit speed } N_{\text{utest}} = 27.4 \text{ rpm/m}^{0.5}$$

$$\text{Normal working head } H_{\text{normal}} = 6 \text{ m}$$

Normal unit speed  $N_{uNormal} = 30.6 \text{ rpm/m}^{0.5}$

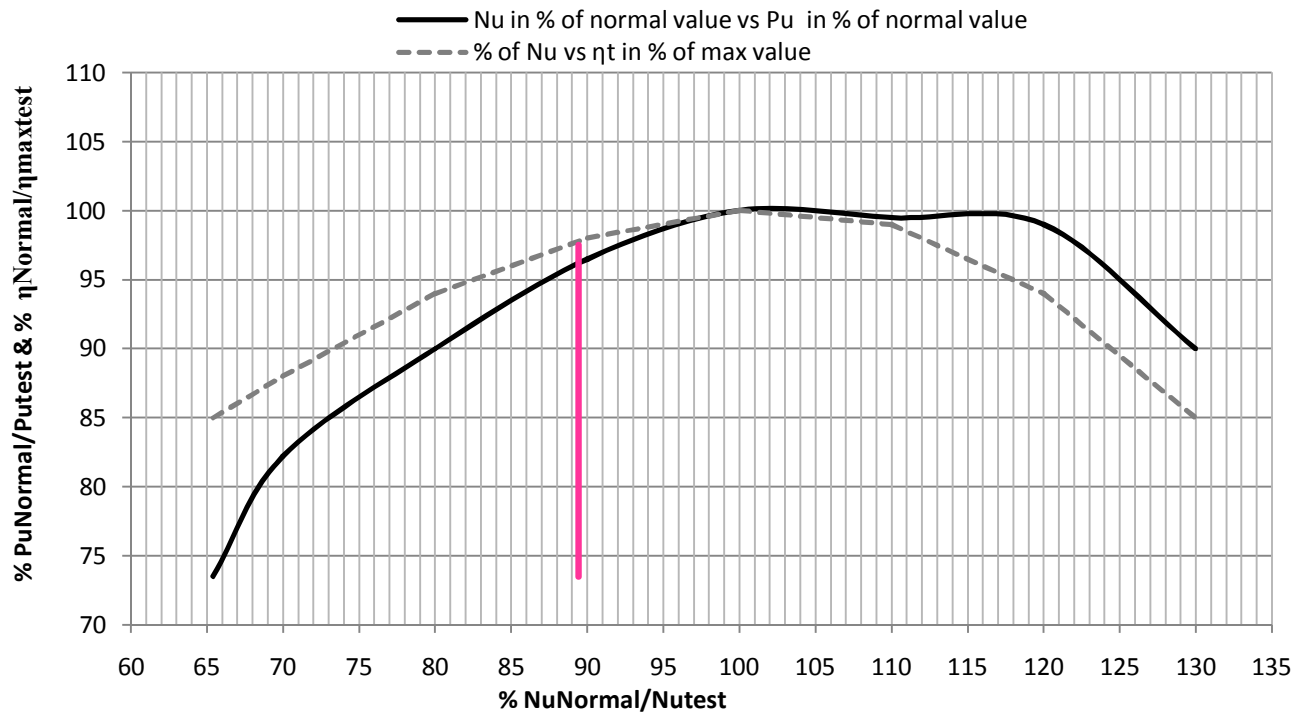
% of tested unit speed  $N_{utest}/N_{uNormal} = 89.4 \%$

efficiency  $\eta$  in % of normal value  
cooresponding to graph  $\eta_{test}/\eta_{Normal} = 96 \%$

Unit power in % of normal value  
cooresponding to graph  $P_{utest}/P_{uNormal} = 97.5 \%$

graph plot

89.4	73.5
89.4	97.5



Normal unit power  $P_{uNormal} = 74.9 \text{ kW/m}^{1.5}$

normal efficiency  $\eta_{normal} = 90.6 \%$

$P_{normal} = (P_{uNormal} * H^{1.5}) = 1100.8 \text{ kW}$

$Q_{normal} = (P_{normal} * 1000 / \gamma \eta_{Normal} H_{normal}) = 20.6 \text{ m}^3/\text{s}$

A small hydro development, a Kaplan turbine runs under a head of 2.1m. It has a runner of 3.5 m diameter and develops 600 kW at 80 r.p.m. Determine the discharge and specific speed of the machine assuming an overall efficiency of 80%. If a homogeneous turbine is to be tested at a head of 3.0 m and diameter 1.5 m, what are the rotational speed, discharge and power of the unit?

$H_p =$  2.1 m p- for prototype

$\eta_{op} =$  80 % m- for model

$P_p =$  600 kW

$N_p =$  80 rpm

$D_p =$  3.5 m

$D_m =$  1.5 m

$H_m =$  3 m

$Q_p =$  36.406 m<sup>3</sup>/s

$Ns_p =$  775.16

for homogeneous turbine,

$N_m =$  223.11 rpm using  $(gH/N^2D^2)_m = (gH/N^2D^2)_p$

$Q_m =$  7.99 m<sup>3</sup>/s using  $(Q/ND^3)_m = (Q/ND^3)_p$

$P_m =$  188.17 kW using  $(P/\rho N^3D^3)_m = (P/\rho N^3D^3)_p$